Chapter Five

MAGNETISM AND MATTER



MCQ I

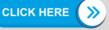
- **5.1** A toroid of n turns, mean radius R and cross-sectional radius a carries current I. It is placed on a horizontal table taken as x-y plane. Its magnetic moment \mathbf{m}
 - (a) is non-zero and points in the z-direction by symmetry.
 - (b) points along the axis of the tortoid ($\mathbf{m} = m \hat{\mathbf{q}}$).
 - (c) is zero, otherwise there would be a field falling as $\frac{1}{r^3}$ at large distances outside the toroid.
 - (d) is pointing radially outwards.
- **5.2** The magnetic field of Earth can be modelled by that of a point dipole placed at the centre of the Earth. The dipole axis makes an angle of 11.3° with the axis of Earth. At Mumbai, declination is nearly zero. Then,
 - (a) the declination varies between 11.3° W to 11.3° E.
 - (b) the least declination is 0° .



- (c) the plane defined by dipole axis and Earth axis passes through Greenwich.
- (d) declination averaged over Earth must be always negative.
- 5.3 In a permanent magnet at room temperature
 - (a) magnetic moment of each molecule is zero.
 - (b) the individual molecules have non-zero magnetic moment which are all perfectly aligned.
 - (c) domains are partially aligned.
 - (d) domains are all perfectly aligned.
- 5.4 Consider the two idealized systems: (i) a parallel plate capacitor with large plates and small separation and (ii) a long solenoid of length L >> R, radius of cross-section. In (i) **E** is ideally treated as a constant between plates and zero outside. In (ii) magnetic field is constant inside the solenoid and zero outside. These idealised assumptions, however, contradict fundamental laws as below:
 - (a) case (i) contradicts Gauss's law for electrostatic fields.
 - (b) case (ii) contradicts Gauss's law for magnetic fields.
 - (c) case (i) agrees with $\iint \mathbf{E} \cdot d\mathbf{l} = 0$.
 - (d) case (ii) contradicts $\iint \mathbf{H} \cdot d\mathbf{l} = I_{en}$
- 5.5 A paramagnetic sample shows a net magnetisation of 8 Am⁻¹ when placed in an external magnetic field of 0.6T at a temperature of 4K. When the same sample is placed in an external magnetic field of 0.2T at a temperature of 16K, the magnetisation will be
 - (a) $\frac{32}{3}$ Am⁻¹
 - (b) $\frac{2}{3}$ Am⁻¹
 - (c) $6 \, \text{Am}^{-1}$
 - (d) 2.4 Am⁻

MCQ II

- S is the surface of a lump of magnetic material.
 - (a) Lines of $\bf B$ are necessarily continuous across $\bf S$.
 - (b) Some lines of $\bf B$ must be discontinuous across $\bf S$.
 - (c) Lines of ${\bf H}$ are necessarily continuous across ${\bf S}$.
 - (d) Lines of \mathbf{H} cannot all be continuous across S.



29

Exemplar Problems-Physics

- 5.7 The primary origin(s) of magnetism lies in
 - (a) atomic currents.
 - (b) Pauli exclusion principle.
 - (c) polar nature of molecules.
 - (d) intrinsic spin of electron.
- A long solenoid has 1000 turns per metre and carries a current of 5.8 1 A. It has a soft iron core of $\mu_{\rm r}$ = 1000 . The core is heated beyond the Curie temperature, T_c .
 - (a) The **H** field in the solenoid is (nearly) unchanged but the **B** field decreases drastically.
 - (b) The **H** and **B** fields in the solenoid are nearly unchanged.
 - (c) The magnetisation in the core reverses direction.
 - (d) The magnetisation in the core diminishes by a factor of about 108.
- 5.9 Essential difference between electrostatic shielding by a conducting shell and magnetostatic shielding is due to
 - (a) electrostatic field lines can end on charges and conductors have free charges.
 - (b) lines of **B** can also end but conductors cannot end them.
 - (c) lines of **B** cannot end on any material and perfect shielding is not possible.
 - (d) shells of high permeability materials can be used to divert lines of **B** from the interior region.
- **5.10** Let the magnetic field on earth be modelled by that of a point magnetic dipole at the centre of earth. The angle of dip at a point on the geographical equator
 - (a) is always zero.
 - (b) can be zero at specific points.
 - (c) can be positive or negative.
 - (d) is bounded.

VSA

- **5.11** A proton has spin and magnetic moment just like an electron. Why then its effect is neglected in magnetism of materials?
- **5.12** A permanent magnet in the shape of a thin cylinder of length 10 cm has $M = 10^6$ A/m. Calculate the magnetisation current I_{M} .
- **5.13** Explain quantitatively the order of magnitude difference between the diamagnetic susceptibility of N_2 (~5 × 10⁻⁹) (at STP) and Cu (~10⁻⁵).



- **5.14** From molecular view point, discuss the temperature dependence of susceptibility for diamagnetism, paramagnetism and ferromagnetism.
- **5.15** A ball of superconducting material is dipped in liquid nitrogen and placed near a bar magnet. (i) In which direction will it move? (ii) What will be the direction of it's magnetic moment?

SA

- **5.16** Verify the Gauss's law for magnetic field of a point dipole of dipole moment **m** at the origin for the surface which is a sphere of radius *R*.
- **5.17** Three identical bar magnets are rivetted together at centre in the same plane as shown in Fig. 5.1. This system is placed at rest in a slowly varying magnetic field. It is found that the system of magnets does not show any motion. The north-south poles of one magnet is shown in the Fig. 5.1. Determine the poles of the remaining two.
- 5.18 Suppose we want to verify the analogy between electrostatic and magnetostatic by an explicit experiment. Consider the motion of (i) electric dipole p in an electrostatic field E and (ii) magnetic dipole m in a magnetic field B. Write down a set of conditions on E, B, p, m so that the two motions are verified to be identical. (Assume identical initial conditions.)
- **5.19** A bar magnet of magnetic moment m and moment of inertia I (about centre, perpendicular to length) is cut into two equal pieces, perpendicular to length. Let T be the period of oscillations of the original magnet about an axis through the mid point, perpendicular to length, in a magnetic field \mathbf{B} . What would be the similar period T' for each piece?
- **5.20** Use (i) the Ampere's law for \mathbf{H} and (ii) continuity of lines of \mathbf{B} , to conclude that inside a bar magnet, (a) lines of \mathbf{H} run from the N pole to S pole, while (b) lines of \mathbf{B} must run from the S pole to N pole.

LA

5.21 Verify the Ampere's law for magnetic field of a point dipole of dipole moment $\mathbf{m} = m\hat{\mathbf{k}}$. Take C as the closed curve running clockwise along (i) the z-axis from z = a > 0 to z = R; (ii) along the quarter circle of radius R and centre at the origin, in the first quadrant of x-z plane; (iii) along the x-axis from x = R to x = a, and (iv) along the quarter circle of radius a and centre at the origin in the first quadrant of x-z plane.

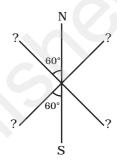


Fig. 5.1



- **5.22** What are the dimensions of χ , the magnetic susceptibility? Consider an H-atom. Guess an expression for χ , upto a constant by constructing a quantity of dimensions of χ , out of parameters of the atom: e, m, v, R and μ_0 . Here, m is the electronic mass, v is electronic velocity, R is Bohr radius. Estimate the number so obtained and compare with the value of $|\chi| \sim 10^{-5}$ for many solid materials.
- **5.23** Assume the dipole model for earth's magnetic field B which is given

by B_V = vertical component of magnetic field = $\frac{\mu_0}{4\pi} \frac{2m\cos\theta}{\mathbf{r}^3}$

 $B_{\rm H}$ = Horizontal component of magnetic field = $\frac{\mu_0}{4\pi} \frac{\sin\theta\,{\rm m}}{r^3}$

 θ = 90° – lattitude as measured from magnetic equator.

Find loci of points for which (i) $|\mathbf{B}|$ is minimum; (ii) dip angle is zero; and (iii) dip angle is \pm 45°.

- **5.24** Consider the plane S formed by the dipole axis and the axis of earth. Let P be point on the magnetic equator and in S. Let Q be the point of intersection of the geographical and magnetic equators. Obtain the declination and dip angles at P and Q.
- **5.25** There are two current carrying planar coils made each from identical wires of length L. C_1 is circular (radius R) and C_2 is square (side a). They are so constructed that they have same frequency of oscillation when they are placed in the same uniform \mathbf{B} and carry the same current. Find a in terms of R.

